

$$\begin{aligned}\mathfrak{S}|_v\mathbb{L} &= \mathfrak{S}_{\pm}^0|_v\mathbb{L} \times \mathfrak{S}^{\times}|_v\mathbb{L} \times \mathfrak{S}^{2\times}|_v\mathbb{L} \\ \mathfrak{S}|_e\mathbb{L} &= \mathfrak{S}_{\pm}^0|_e\mathbb{L} \times \mathfrak{S}^{\times}|_e\mathbb{L} \times \mathfrak{S}^{2\times}|_e\mathbb{L}\end{aligned}$$

$$\mathfrak{S}_1^o|_v\mathbb{L}=\frac{\delta\in\mathsf{E}(\mathbb{L})}{e\delta=0}=\mathsf{E}(\mathbb{L}:e)$$

$$\delta \rtimes g_e = \delta$$

$$\mathfrak{S}^o_-|_v\mathbb{L}=\frac{a-z\overset{*}{a}z\partial_z}{a=\overset{*}{a}\in U}\times\frac{c-z\overset{*}{c}z\partial_z}{c\in W}$$

$$\underline{a-z\overset{*}{a}z}\rtimes g_e=2\overset{*}{e}a:\;\;\;\underline{c-z\overset{*}{c}z}\rtimes g_e=c-z\overset{*}{c}z$$

$$\mathfrak{S}^{\times}|_v\mathbb{L}=\frac{\overbrace{b-z\overset{*}{b}z+2\kappa z\overset{*}{b}e-z\overset{*}{e}b}^{\lambda}\partial_z}{b\in V}$$

$$\begin{aligned}\overbrace{b-z\overset{*}{b}z+2\underline{z\overset{*}{b}e-z\overset{*}{e}b}}^{\lambda}\rtimes g_e &= \sqrt{2}\underline{b+2\overset{*}{b}e}, \\ \overbrace{b-z\overset{*}{b}z-2\underline{z\overset{*}{b}e-z\overset{*}{e}b}}^{\lambda}\rtimes g_e &= -\sqrt{2}\underline{b+2\overset{*}{e}b}\end{aligned}$$

$$\mathfrak{S}^{2\times}|_v\mathbb{L}=\frac{a-z\overset{*}{a}z+2\kappa z\overset{*}{a}e\partial_z}{a=-\overset{*}{a}\in U}$$

$$\begin{aligned}\underline{a-z\overset{*}{a}z+2z\overset{*}{a}e}\rtimes g_e &= 2a \\ 2\overset{*}{a}e &= \overset{*}{a}e-\overset{*}{e}a \\ \underline{a-z\overset{*}{a}z-2z\overset{*}{a}e}\rtimes g_e &= -2\overset{*}{a}\end{aligned}$$

$$\mathfrak{S}^{\lambda}|_v\mathbb{L}=\frac{\mathfrak{b}\in\mathfrak{S}|_v\mathbb{L}}{\mathfrak{b}\rtimes\underbrace{e-\overset{*}{e}}_{\lambda\mathfrak{b}}=\lambda\mathfrak{b}}$$

$$\overbrace{X_u^-+\alpha\underbrace{\overset{*}{ue}-\overset{*}{eu}}_{\overset{*}{e\dot{e}u}-\overset{*}{e\ddot{e}e}}}^{\lambda}\rtimes X_e^-=2\underbrace{\overset{*}{ue}-\overset{*}{eu}}_{\overset{*}{e\dot{e}u}-\overset{*}{e\ddot{e}e}}+\alpha X_{\overset{*}{e\dot{e}u}-\overset{*}{e\ddot{e}e}}^-=\lambda\overbrace{X_u^-+\alpha\underbrace{\overset{*}{ue}-\overset{*}{eu}}_{\overset{*}{e\dot{e}u}-\overset{*}{e\ddot{e}e}}}$$

$$u = \overset{*}{\dot{u}} \in U \Rightarrow \overset{*}{\dot{u}}e - \overset{*}{\dot{e}}u = 0$$

$$e\overset{*}{\dot{e}}u - e\overset{*}{\dot{u}}e = u - \overset{*}{\dot{u}} = 0 \Rightarrow \lambda = 0 = \alpha$$

$$u = -\overset{*}{\dot{u}} \in U \Rightarrow e\overset{*}{\dot{e}}u - e\overset{*}{\dot{u}}e = u - \overset{*}{\dot{u}} = 2u \Rightarrow \lambda = 2\alpha$$

$$\lambda\alpha = 2 \Rightarrow \begin{cases} \alpha = 1 & \lambda = 2 \\ \alpha = -1 & \lambda = -2 \end{cases}$$

$$u \in V \Rightarrow \overset{*}{\dot{e}}u - e\overset{*}{\dot{u}}e = u/2 \Rightarrow \lambda = \alpha/2$$

$$\lambda\alpha = 2 \Rightarrow \begin{cases} \alpha = 2 & \lambda = 1 \\ \alpha = -2 & \lambda = -1 \end{cases}$$