

$$\begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \\ \hline 0 & \pm \\ \hline -\pm & 0 \end{array} \xrightarrow{\quad} \begin{cases} {}^n\mathbb{C}_{\mathbb{R}^n}^{\mathbb{C}} \\ {}^n\mathbb{H}_{\mathbb{C}^n}^{\mathbb{C}} \end{cases}$$

$$\Gamma = a + bi \Rightarrow \overset{*}{\Gamma} = \overset{*}{a} - \overset{*}{b}i \Rightarrow \underset{\mathbb{R}}{\Gamma} = \frac{a}{-b} \left| \begin{array}{c} b \\ a \end{array} \right. \xrightarrow{*_{\text{hom}}} \underset{\mathbb{R}}{\overset{*}{\Gamma}} = \frac{a}{-b} \left| \begin{array}{c} b \\ \overset{*}{a} \end{array} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \begin{array}{c} -\overset{*}{b} \\ \overset{*}{a} \end{array} \right. = \frac{\overset{*}{a} - \overset{*}{b}i}{\mathbb{C}} = \underset{\mathbb{R}}{\overset{*}{\Gamma}}$$

$$\Gamma = a + bj \Rightarrow \overset{*}{\Gamma} = \overset{*}{a} - j\overset{*}{b} = \overset{*}{a} - \overset{+}{b}j \Rightarrow \underset{\mathbb{C}}{\Gamma} = \frac{a}{-\bar{b}} \left| \begin{array}{c} b \\ \bar{a} \end{array} \right. \xrightarrow{*_{\text{hom}}} \underset{\mathbb{C}}{\overset{*}{\Gamma}} = \frac{a}{-\bar{b}} \left| \begin{array}{c} b \\ \overset{*}{\bar{a}} \end{array} \right. = \frac{\overset{*}{a}}{\overset{*}{b}} \left| \begin{array}{c} -\overset{*}{b} \\ \overset{+}{\bar{a}} \end{array} \right. = \frac{\overset{*}{a} - \overset{+}{b}j}{\mathbb{C}} = \underset{\mathbb{C}}{\overset{*}{\Gamma}}$$

$$\begin{array}{c|c} 1 & 0 \\ \hline 0 & -1 \end{array} \xrightarrow{\quad} {}^n\mathbb{R}_{\mathbb{R}^n}^{\mathbb{C}}$$

$$\begin{cases} {}^n\mathbb{C}_{\mathbb{R}^n}^{\mathbb{C}} \\ {}^n\mathbb{H}_{\mathbb{C}^n}^{\mathbb{C}} \end{cases} = \begin{cases} \Gamma \in {}^n\mathbb{R}_{\mathbb{R}^n}^{\mathbb{C}} & \Gamma \left| \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \end{array} \\ \hline 0 & 0 \\ \hline -1 & 0 \end{array} \right. = \left| \begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \end{array} \right| \Gamma \\ \Gamma \in {}^n\mathbb{C}_{\mathbb{C}^n}^{\mathbb{C}} & \Gamma \left| \begin{array}{c|c} 0 & \begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \end{array} \\ \hline 0 & 0 \\ \hline -1 & 0 \end{array} \right. = \left| \begin{array}{c|c} 0 & 1 \\ \hline -1 & 0 \end{array} \right| \Gamma \end{cases}$$

$$\begin{array}{c|cc} \bar{\sigma} & -\sigma i \\ \hline -i\bar{\sigma} & \sigma \end{array} \quad {}^n\mathbb{C}_n^{\mathbb{C}} \begin{array}{c|cc} \sigma & \sigma i \\ \hline i\bar{\sigma} & \bar{\sigma} \end{array} = {}^n\mathbb{K}_n^{\mathbb{C}}$$

$$\Gamma = a + bi \in {}^n\mathbb{C}_n^{\mathbb{C}} \Rightarrow \underline{\Gamma} = \begin{array}{c|c} \bar{\Gamma} & 0 \\ \hline 0 & \Gamma \end{array} = \underline{\Gamma}_{\mathbb{C}}$$

$$\begin{array}{c|cc} \bar{\sigma} & -\sigma i \\ \hline -i\bar{\sigma} & \sigma \end{array} \begin{array}{c|cc} a - bi & 0 \\ \hline 0 & a + bi \end{array} \begin{array}{c|cc} \sigma & \sigma i \\ \hline i\bar{\sigma} & \bar{\sigma} \end{array} = \begin{array}{c|cc} \bar{\sigma} & -\sigma i \\ \hline -i\bar{\sigma} & \sigma \end{array} \underline{\Gamma} \begin{array}{c|cc} \sigma & \sigma i \\ \hline i\bar{\sigma} & \bar{\sigma} \end{array} = \underline{\Gamma}_{\mathbb{R}} = \begin{array}{c|cc} a & b \\ \hline -b & a \end{array}$$

$$\sigma \in \mathbb{C}^{\mathbb{U}} \Rightarrow \begin{cases} \begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline \kappa\bar{\sigma} & \kappa j\bar{\sigma} \end{array} {}^n\mathbb{H}_n^{\mathbb{C}} \begin{array}{c|cc} \sigma & \kappa\sigma \\ \hline \sigma j & -\kappa\sigma j \end{array} = {}^n\mathbb{X}_n^{\mathbb{C}} & {}^n\mathbb{H}_n^{\mathbb{C}} = \begin{array}{c|cc} \sigma & \kappa\sigma \\ \hline \sigma j & -\kappa\sigma j \end{array} {}^n\mathbb{H}_n^{\mathbb{C}} \begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline \kappa\bar{\sigma} & \kappa j\bar{\sigma} \end{array} \\ {}^n\mathbb{H}_n^{\mathbb{C}} = \begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline -\kappa i\bar{\sigma} & \kappa j i\bar{\sigma} \end{array} {}^n\mathbb{H}_n^{\mathbb{C}} \begin{array}{c|cc} \sigma & \kappa\sigma i \\ \hline \sigma j & \kappa\sigma ij \end{array} & \begin{array}{c|cc} \sigma & \kappa\sigma i \\ \hline \sigma j & \kappa\sigma ij \end{array} {}^n\mathbb{H}_n^{\mathbb{C}} \begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline -\kappa i\bar{\sigma} & \kappa j i\bar{\sigma} \end{array} = {}^n\mathbb{H}_n^{\mathbb{C}} \end{cases}$$

$$\begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline \kappa\bar{\sigma} & \kappa j\bar{\sigma} \end{array} \begin{array}{c|cc} a & b \\ \hline -b & \bar{a} \end{array} \begin{array}{c|cc} \sigma & \kappa\sigma \\ \hline \sigma j & -\kappa\sigma j \end{array} \underset{\text{unit}}{=} \begin{array}{c|cc} a + bj & 0 \\ \hline 0 & a - bj \end{array}$$

$$\Gamma = a + bj \in {}^n\mathbb{H}_n^{\mathbb{C}} \Rightarrow \underline{\Gamma} i \underline{\Gamma}^* = i \Rightarrow \underline{\Gamma}^{*-1} = -i \underline{\Gamma} i = -i \underline{a + bj} i = a - bj$$

$$\begin{array}{c|cc} \bar{\sigma} & -j\bar{\sigma} \\ \hline -\kappa i\bar{\sigma} & \kappa j i\bar{\sigma} \end{array} \begin{array}{c|cc} a & b \\ \hline -b & \bar{a} \end{array} \begin{array}{c|cc} \sigma & \kappa\sigma i \\ \hline \sigma j & \kappa\sigma ij \end{array} = \begin{array}{c|cc} a + bj & 0 \\ \hline 0 & a + bj \end{array}$$

$$\Gamma \in {}^n\mathbb{K}_n^{\mathbb{C}} \Rightarrow \underline{\Gamma} = \begin{array}{c|cc} \Gamma & 0 \\ \hline 0 & \Gamma^{-1} \end{array} \Rightarrow \begin{cases} \begin{array}{c|cc} \Gamma^* & 0 \\ \hline 0 & \Gamma^{-1} \end{array} \\ \begin{array}{c|cc} \Gamma^{-1} & 0 \\ \hline 0 & \Gamma \end{array} \end{cases}$$