

$$^a\overline{\partial_p\mathfrak{I}}=\,^0\overline{a\ltimes\overline{\partial_p\mathfrak{I}}}=\,^0\overline{\partial_p\underline{a\ltimes\mathfrak{I}}}=p\ltimes\underline{a\ltimes\mathfrak{I}}$$