

$$\mathbb{C} \supset K \text{ comp}$$

$$\partial K \text{ stw glatt}$$

$$\gamma \in {}^K \triangle_{\infty} \mathbb{C} \Rightarrow \int_{dw}^{\partial K} {}^w \gamma = 2i \int_{dxdy}^K \bar{\partial}_z \gamma = \int_{d\bar{z}dz}^K \bar{\partial}_z \gamma$$

$$z = x + iy \Rightarrow \begin{cases} 2idx \times dy = \underbrace{dx - idy} \times \underbrace{dx + idy} = d\bar{z} \times dz \\ 2idxdy = d\bar{z}dz \end{cases}$$

$$d(\gamma dz) = d\gamma \times dz = \left(\partial_z \gamma dz + \bar{\partial}_z \gamma d\bar{z}\right) \times dz = \bar{\partial}_z \gamma d\bar{z} \times dz = 2i \bar{\partial}_z \gamma dx \times dy$$

$$d(\gamma dz) = d(\gamma dx + i\gamma dy) = \partial_y \gamma dy \times dx + i \partial_x \gamma dx \times dy = \left(i\partial_x \gamma - \partial_y \gamma\right) dx \times dy$$

$$\gamma \in {}^{a||b} \triangle_{\infty} \mathbb{C} \Rightarrow \int_{dw}^{\partial a||b} \gamma = 2i \int_{dxdy}^{a||b} \bar{\partial}_z \gamma = \int_{d\bar{z}dz}^{a||b} \bar{\partial}_z \gamma$$

$$\begin{aligned} 2i \int_{dxdy}^{a||b} \bar{\partial}_z \gamma &= \int_{dxdy}^{a||b} (i\partial_x \gamma - \partial_y \gamma) = i \int_{dy}^{\mathcal{I}a|\mathcal{I}b} \int_{dx}^{\Re a|\Re b} \partial_x \gamma - \int_{dx}^{\Re a|\Re b} \int_{dy}^{\mathcal{I}a|\mathcal{I}b} \partial_y \gamma = \\ i \int_{dy}^{\mathcal{I}a|\mathcal{I}b} \underbrace{\Re b + iy \gamma - \Re a + iy \gamma}_{\Re a|\Re b} - \int_{dx}^{\Re a|\Re b} \underbrace{x + i\mathcal{I}b \gamma - x + i\mathcal{I}a \gamma}_{\partial a||b} &= \int_{dw}^{\partial a||b} \gamma \end{aligned}$$

$$\mathbb{C} \supset \tilde{\mathbb{C}}_{\varrho:R} \text{ comp}$$

$$\tilde{\mathbb{C}}_{\varrho:R} \text{ stw glatt}$$

$$\gamma \in \tilde{\mathbb{C}}_{\varrho:R} \rightrightarrows \mathbb{C} \Rightarrow \int_{dw}^{\tilde{\mathbb{C}}_{\varrho:R}} \gamma = 2i \int_{dxdy}^{\tilde{\mathbb{C}}_{\varrho:R}} \bar{\partial}_z \gamma = \int_{d\bar{z}dz}^{\tilde{\mathbb{C}}_{\varrho:R}} \bar{\partial}_z \gamma$$

$$z = x + iy = o + r^{it} \mathfrak{e} = o + r^t \mathfrak{c} + ir^t \mathfrak{s}$$

$$\partial_r \gamma = \underbrace{\partial_x \gamma}_{\partial_r x} + \underbrace{\partial_y \gamma}_{\partial_r y} = \underbrace{\partial_x \gamma}_{\partial_r x}^t \mathfrak{c} + \underbrace{\partial_y \gamma}_{\partial_r y}^t \mathfrak{s}$$

$$\partial_t \gamma = \underbrace{\partial_x \gamma}_{\partial_t x} + \underbrace{\partial_y \gamma}_{\partial_t y} = -r \underbrace{\partial_x \gamma}_{\partial_t x}^t \mathfrak{s} + r \underbrace{\partial_y \gamma}_{\partial_t y}^t \mathfrak{c}$$

$$\partial_r \gamma + \frac{i}{r} \underbrace{\partial_t \gamma}_{\partial_t x} = \underbrace{\partial_x \gamma}_{\partial_t x}^t \mathfrak{c} - \underbrace{i^t \mathfrak{s}}_{\partial_t y} + i \underbrace{\partial_y \gamma}_{\partial_t y}^t \mathfrak{c} - \underbrace{i^t \mathfrak{s}}_{\partial_t x} = 2 \underbrace{\bar{\partial}_z \gamma}_{\partial_t x} e^{-it}$$

$$\Rightarrow 2ir \underbrace{\bar{\partial}_z \gamma}_{\partial_t x} = i e^{it} \underbrace{r \partial_r \gamma + i \partial_t \gamma}_{\partial_t x} = ir e^{it} \underbrace{\partial_r \gamma}_{\partial_t x} - e^{it} \underbrace{\partial_t \gamma}_{\partial_t x} = i e^{it} \overline{\partial_r x \gamma} - \partial_t e^{it} \gamma$$

$$2i \int_{dxdy}^{\tilde{\mathbb{C}}_{\varrho:R}} \bar{\partial}_z \gamma = 2i \int_{rdr}^{\varrho|R} \int_{dt}^{0|2\pi} \bar{\partial}_z \gamma = i \int_{dt}^{0|2\pi} e^{it} \int_{dr}^{\varrho|R} \partial_r x \gamma - \int_{dr}^{\varrho|R} \int_{dt}^{0|2\pi} \partial_t e^{it} \gamma \stackrel{\text{HS}}{=}$$

$$i \int_{dt}^{0|2\pi} e^{it} \underbrace{x \gamma}_{\varrho}^R - \int_{dr}^{\varrho|R} \underbrace{e^{it} \gamma}_{\substack{0 \\ =0}}^{2\pi} = i \int_{dt}^{0|2\pi} e^{it} \underbrace{R^{o+Re^{it}} \gamma - \varrho^{o+\varrho e^{it}} \gamma}_{\substack{0 \\ =0}} = \int_{dw}^{\tilde{\mathbb{C}}_{\varrho:R}} \gamma$$