

$$\begin{aligned}
& \underbrace{\mathbf{j} \times \mathbf{j}}_{x+iy} = \int_{d\dot{x}/\dot{x}^2 d\dot{y}} \int_{d\ddot{x}/\ddot{x}^2 d\ddot{y}} \mathbf{j}_{\dot{x}+i\dot{y}} \mathbf{j}_{\ddot{x}+i\ddot{y}} \\
& \exp \left(\frac{(\dot{x}^2 - \ddot{x}^2) y + (\ddot{x}^2 - x^2) \dot{y} + (x^2 - \dot{x}^2) \ddot{y}}{x \dot{x} \ddot{x}} \right) \frac{(x^2 + \dot{x}^2)(x^2 + \ddot{x}^2)}{x^2 \dot{x} \ddot{x}} \\
e \underbrace{\mathbf{j} \times \mathbf{j}}_{d\dot{x}/\dot{x}^2 d\dot{y} d\ddot{x}/\ddot{x}^2 d\ddot{y}} &= \int_{d\dot{x}/\dot{x}^2 d\dot{y}} \int_{d\ddot{x}/\ddot{x}^2 d\ddot{y}} \mathbf{j}_{\dot{x}+i\dot{y}} \mathbf{j}_{\ddot{x}+i\ddot{y}} \exp \left(\frac{(\ddot{x}^2 - 1) \dot{y} + (1 - \dot{x}^2) \ddot{y}}{\dot{x} \ddot{x}} \right) \frac{(1 + \dot{x}^2)(1 + \ddot{x}^2)}{\dot{x} \ddot{x}} \\
&= \int_{d\dot{x}/\dot{x}^2 d\dot{y}} \int_{d\ddot{x}/\ddot{x}^2 d\ddot{y}} \mathbf{j}_{\dot{x}+i\dot{y}} \mathbf{j}_{\ddot{x}+i\ddot{y}} \exp \left((\ddot{x} - \ddot{x}^{-1}) \frac{\dot{y}}{\dot{x}} + (\dot{x}^{-1} - \dot{x}) \frac{\ddot{y}}{\ddot{x}} \right) (\dot{x}^{-1} + \dot{x})(\ddot{x}^{-1} + \ddot{x})
\end{aligned}$$